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## A FIXED POINT APPROACH TO THE STABILITY OF $\varphi$ -MORPHISMS ON HILBERT $C^*$ -MODULES

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ABSTRACT. Let E, F be two Hilbert  $C^*$ -modules over  $C^*$ -algebras A and B respectively. In this paper, by the alternative fixed point theorem, we give the Hyers-Ulam-Rassias stability of the equation

$$\langle U(x), U(y) \rangle = \varphi(\langle x, y \rangle) \qquad (x, y \in E),$$

where  $U: E \to F$  is a mapping and  $\varphi: A \to B$  is an additive map.

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