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## ON THE SUZUKI NONEXPANSIVE-TYPE MAPPINGS

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ABSTRACT. It is shown that if  $C$  is a nonempty convex and weakly compact subset of a Banach space  $X$  with  $M(X) > 1$  and  $T : C \rightarrow C$  satisfies condition  $(C)$  or is continuous and satisfies condition  $(C_\lambda)$  for some  $\lambda \in (0, 1)$ , then  $T$  has a fixed point. In particular, our theorem holds for uniformly nonsquare Banach spaces. A similar statement is proved for nearly uniformly noncreasy spaces.

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