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## COMPOSITION OPERATORS ACTING BETWEEN SOME WEIGHTED MÖBIUS INVARIANT SPACES

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ABSTRACT. In this paper we investigate conditions under which a holomorphic self-map of the unit disk induces a composition operator  $C_{\phi}$  with closed range on the weighted Bloch space  $\mathcal{B}_{\log}$ . Also, we introduce a new class of functions the so called  $F_{\log}(p,q,s)$  spaces. Necessary and sufficient conditions are given for a composition operator  $C_{\phi}$  to be bounded and compact from  $\mathcal{B}_{\log}$  to  $F_{\log}(p,q,s)$ . Moreover, necessary and sufficient conditions for  $C_{\phi}$  from the Dirichlet space  $\mathcal{D}$  to the spaces  $F_{\log}(p,q,s)$  to be compact are given in terms of the map  $\phi$ .

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