



EXPLICIT DESCRIPTION OF SOME CLASSES OF NON-BENDING SURFACES

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Abstract. Here we consider a family of axially symmetric surfaces modeling the shape of thin mechanical shells that are deformable without bending under uniform loading. With the exception of very few surfaces, like the well known right circular cylinder and the sphere, the surfaces of this family have no closed form description in elementary functions. Our main goal is to present their explicit parameterizations including both classes of open and closed families. We distinguish four classes of non-bending surfaces differing by their canonical representations using the normal elliptic integrals and the Jacobian elliptic functions.

MSC: 74K25, 74A10, 53A04, 53A05, 33E05

Keywords: Axially symmetric surfaces, bending of shells, elliptic integrals, parameterizations, stress analysis, surface geometry

Contents

1	Introduction	43
2	Reduction to the Canonical Forms	47
3	Non-Bending Surfaces of the First Class $\mathcal{S}^I(\nu)$	53
4	Non-Bending Surfaces of the Second Class $\mathcal{S}^{II}(\nu)$	58
5	Non-Bending Surfaces of the Third Class $\mathcal{S}^{III}(\nu)$	61
6	Non-Bending Surfaces of the Fourth Class $\mathcal{S}^{IV}(\nu)$	65
7	Comments	68
	References	70