Corrections to Article 16.5.5

Lin Jiu and Christophe Vignat

September 23, 2019

We apologize for a mistake in the example in part (III) of Remark 9. Therefore, we shall make the following corrections.

1. Equation (14) in Theorem 8 should be

$$\binom{m+n}{r}_{b} = \sum_{k=0}^{r} \binom{m}{k}_{b} \binom{n}{r-k}_{b}.$$

2. At the end of the proof of Theorem 8, the following paragraph should be added:

Note that the summation condition $0 \le k \le_b r$ can be replaced by $0 \le k \le r$, since when k + (r - k) is not carry-free, it means that $k_j > r_j$ for some $j \in \{0, \ldots, N - 1\}$. In this case,

$$\binom{n}{r-k}_{b} = \left(\prod_{l=0}^{j-1} \binom{n_{l}}{r_{l}-k_{l}}\right) \binom{n_{j}}{r_{j}-k_{j}} \left(\prod_{l=j+1}^{N-1} \binom{n_{l}}{r_{l}-k_{l}}\right) = 0,$$

and the corresponding term has no contribution to the sum.

3. Part (III) of Remark 9 should be removed.